

(* 1. zadatak: $X = (A^T - 2E)^{-1} B^{-1} = (B(A^T - 2E))^{-1} = M^{-1}$ *)

$A = \{\{0, 2, -1\}, \{0, 1, 0\}, \{1, -1, 3\}\}$

$\{\{0, 2, -1\}, \{0, 1, 0\}, \{1, -1, 3\}\}$

$B = \{\{2, 1, 0\}, \{1, 0, 1\}, \{0, 0, -1\}\}$

$\{\{2, 1, 0\}, \{1, 0, 1\}, \{0, 0, -1\}\}$

$M = B \cdot (\text{Transpose}[A] - 2 \text{IdentityMatrix}[3])$

$\{\{-2, -1, 1\}, \{-3, 0, 2\}, \{1, 0, -1\}\}$

$X = \text{Inverse}[M]$

$\{\{0, -1, -2\}, \{-1, 1, 1\}, \{0, -1, -3\}\}$

(* 2. zadatak, može da se reši pomoću Kramerovog pravila: *)

$\Delta = \text{Det}[\{\{1, m, -1\}, \{m, 1, -1\}, \{1, -1, m\}\}]$

$m - m^3$

$\Delta_x = \text{Det}[\{\{1, m, -1\}, \{1, 1, -1\}, \{-1, -1, m\}\}]$

$-1 + 2m - m^2$

$\Delta_y = \text{Det}[\{\{1, 1, -1\}, \{m, 1, -1\}, \{1, -1, m\}\}]$

$-1 + 2m - m^2$

$\Delta_z = \text{Det}[\{\{1, m, 1\}, \{m, 1, 1\}, \{1, -1, -1\}\}]$

$-1 + m^2$

(* 1. slučaj za $\Delta \neq 0 \Leftrightarrow m \neq 0, 1, -1$ sistem ima jedinstveno rešenje*)

$\{x, y, z\} = \{\text{Simplify}[\Delta_x / \Delta], \text{Simplify}[\Delta_y / \Delta], \text{Simplify}[\Delta_z / \Delta]\}$

$\left\{ \frac{-1+m}{m(1+m)}, \frac{-1+m}{m(1+m)}, -\frac{1}{m} \right\}$

(* 2. slučaj, za $m=0$ ili $m=-1$ je $\Delta_x \neq 0$ i $\Delta=0$ pa sistem nema rešenja *)

(* 3. slučaj, za $m=1$ sve determinante su 0,

pa zamenjujemo $m=1$ u polazni sistem i radimo Gausov metod eliminacije: *)

$\text{Clear}[x, y, z]$

$\text{Solve}[\{x+y-z == 1 \ \&\& \ x+y-z == 1 \ \&\& \ x-y+z == -1\}, \{x, y, z\}]$

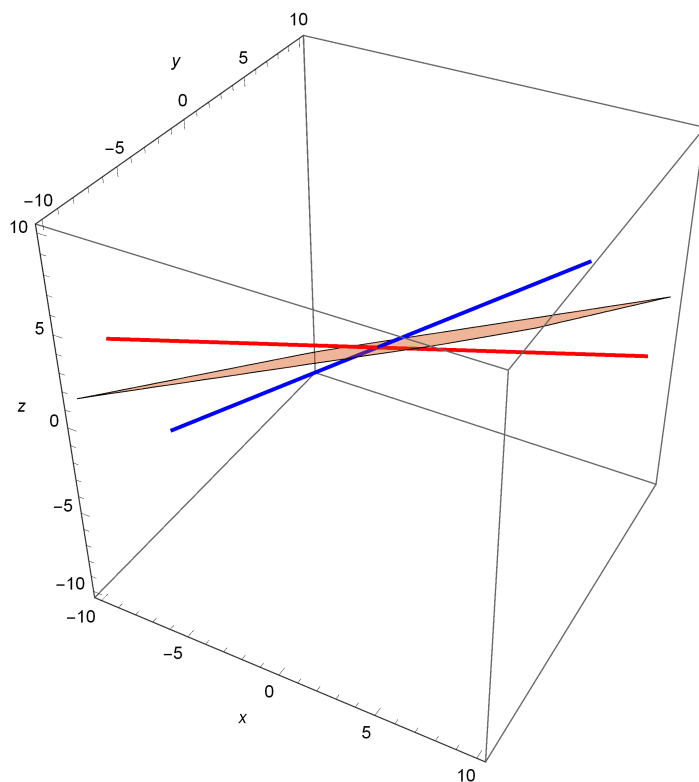
$\text{Solve}::\text{svars}$: Equations may not give solutions for all "solve" variables. >>

$\{\{x \rightarrow 0, z \rightarrow -1+y\}\}$

(* Sistem ima beskonacno mnogo resenja, $(x, y, z) \in \{(0, t, -1+t) \mid t \in \mathbb{R}\}$ za $m=1$. *)

(* 3. zadatak: prava p (plavo) i njena
projekcija p' (crveno) u odnosu na ravan α na slici *)

```
Show[ $\alpha$  = ContourPlot3D[x - y - 2 z == -3, {x, -10, 10},
  {y, -10, 10}, {z, -10, 10}, AxesLabel -> {x, y, z}, Mesh -> None,
  ContourStyle -> Directive[Orange, Opacity[0.4], Specularity[White, 30]]],
p = ParametricPlot3D[{t, 2 t - 1, 2}, {t, -10, 10},
  PlotStyle -> RGBColor[0, 0, 1], AxesLabel -> {x, y, z}],
p' = ParametricPlot3D[{4 t, 5 t - 1, -2 t + 2}, {t, -10, 10},
  PlotStyle -> RGBColor[1, 0, 0], AxesLabel -> {x, y, z}]]
```



(* 4. zadatak: prava q (plavo), ravan α (narandzasto), ravan β koja sadrzi q i normalna je na α (zeleno). Trazena prava p (crveno) prolazi kroz tacku $M(0,0,-1)$ i ima pravac ortogonalne projekcije q na α ($q'=\alpha \cap \beta$). *)

```
Show[α = ContourPlot3D[2 x + 3 y - z - 1 == 0, {x, -10, 10},
  {y, -10, 10}, {z, -10, 10}, AxesLabel → {x, y, z}, Mesh → None,
  ContourStyle → Directive[Orange, Opacity[0.4], Specularity[White, 30]]],
β = ContourPlot3D[-5 x + 3 y - z + 6 == 0, {x, -10, 10}, {y, -10, 10},
  {z, -10, 10}, AxesLabel → {x, y, z}, Mesh → None,
  ContourStyle → Directive[Green, Opacity[0.4], Specularity[White, 30]]],
q = ParametricPlot3D[{t + 3, 2 t + 3, t}, {t, -10, 10},
  PlotStyle → RGBColor[0, 0, 1], AxesLabel → {x, y, z}],
p = ParametricPlot3D[{0, t, 3 t - 1}, {t, -10, 10},
  PlotStyle → RGBColor[1, 0, 0], AxesLabel → {x, y, z}]]
```

